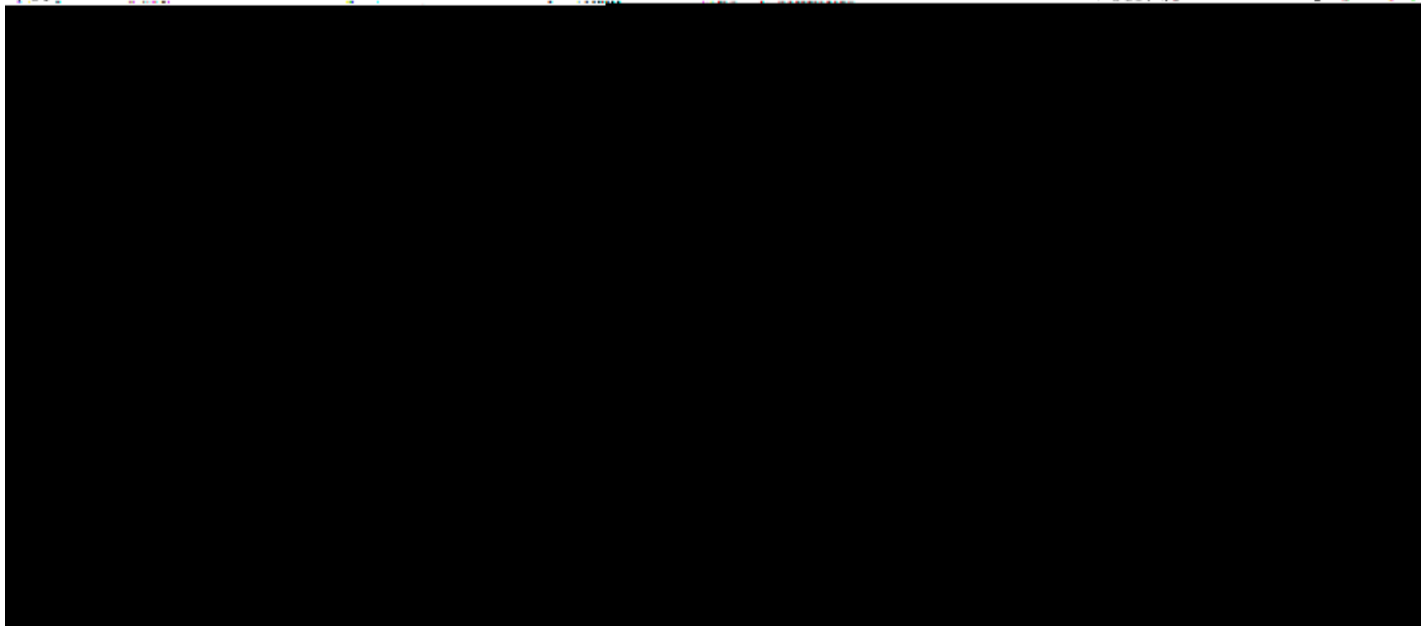


# MAXIMA AND MINIMA

**Absolute Maximum:** Let  $f$  be defined on an interval  $I$  and



**Example:** Locate the absolute and local maxima and minima on the graph of the function

Solution: Absolute maximums at  $x = -2$  and  $x = 2$ .

Absolute and local minimums at  $x = 0$ .

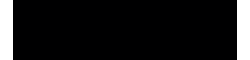
No local maximums.

and there exists a point  $c \in I$  (element of  $I$ ), then  $c$  is a Critical Point. Let  $f$  be defined on an interval  $I$ , a local maximum or minimum at  $c \in I$  if there exists a neighborhood  $N(c)$  such that  $f(c) \geq f(x)$  or  $f(c) \leq f(x)$  for all  $x \in N(c)$ .



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# MAXIMA AND MINIMA

on the interval  $[-1, 2]$  b.)  $g(x) = x^{2/3}(2 - x)$

Solution:

polynomial, thus its derivative exists everywhere. Now let's find the critical points. a.) We know that  $f$  is a polynomial, thus its derivative exists everywhere. Now let's find the critical points:  $x = 0$  and  $x = 3/2$ , and both of these points are...

b.) Given  $g(x) = x^{2/3}(2 - x)$ , we will differentiate this function to find the critical points.  $g'(x) = \frac{2}{3}x^{-1/3}(2 - x) - x^{2/3}$ . So,  $g'(x) = 0 \Rightarrow 4 - 5x = 0 \Rightarrow x = 4/5$ . Thus we have two critical points:  $x = 0$  and  $x = 4/5$ . Now we will check the values of the function at the critical points and the endpoints, i.e.,  $x = -1$  and  $x = 2$ .

Thus we see that the function attains the largest value at  $x = -1$  and the smallest at  $x = 0$  and absolute minimum of  $g$  on  $[-1, 2]$  is 0.

$g(-1) = 3$ ,  $g(0) = 0$ ,  $g(4/5) = 1.03$  and  $g(2) = 0$ . Therefore, absolute maximum of  $g$  on  $[-1, 2]$  is 3 and

